

How Do We Solve A System Of Linear Equations Algebraically?
Substitution Method

* The substitution method is used to eliminate one of the variables by replacement.

Procedure:

- 1) Make sure one variable is alone (ex $x = \dots$, $y = \dots$, $a = \dots$ etc)
- 2) Substitute (replace) that variable's equivalent expression into the other equation (using parentheses) so that we have one equation with one variable.
- 3) Solve for the variable
- 4) Substitute that value back into either original equation and solve for the second variable.
- 5) Check both answers back into both equations.

Solve each system of linear equations using the substitution method and check your answer.

DCMS

1) $x = -2y$
 $5x - 3y = 13$

$5x - 3y = 13$
 $5(-2y) - 3y = 13$
 $-10y - 3y = 13$
 $-13y = 13$
 $-13 \quad -13$
 $y = -1$

$x = -2y$
 $x = -2(-1)$
 $x = 2$

$(2, -1)$

check 1 $(2, -1)$

$x = -2y$
 $2 = -2(-1)$
 $2 = 2$
 \checkmark

check 2 $(2, -1)$

$5x - 3y = 13$
 $5(2) - 3(-1) = 13$
 $10 + 3 = 13$
 $13 = 13$

DCMS

2) $x + y = 1$
 $x = 9 - 3y$

$x + y = 1$
 $9 - 3y + y = 1$
 $9 - 2y = 1$
 $-9 \quad -9$
 $-2y = -8$
 $-2 \quad -2$
 $y = 4$

$x = 9 - 3y$
 $x = 9 - 3(4)$
 $x = 9 - 12$
 $x = -3$

$(-3, 4)$

check 1 $(-3, 4)$

$x + y = 1$
 $-3 + 4 = 1$
 $1 = 1$
 \checkmark

check 2 $(-3, 4)$

$x = 9 - 3y$
 $-3 = 9 - 3(4)$
 $-3 = 9 - 12$
 $-3 = -3$
 \checkmark

3) $y = 3x - 1$
 $7x + 2y = 37$

D $7x + 2y = 37$
 C $7x + 2(3x - 1) = 37$
 M $7x + 6x - 2 = 37$
 S $13x - 2 = 37$
 $\quad +2 \quad +2$
 $\frac{13x = 39}{13 \quad 13}$
 $x = 3$

$y = 3x - 1$
 $y = 3(3) - 1$
 $y = 9 - 1$
 $y = 8$
 $(3, 8)$

chk#1 (3,8)
 $y = 3x - 1$
 $8 = 3(3) - 1$
 $8 = 9 - 1$
 $8 = 8$

chk#2 (3,8)
 $7x + 2y = 37$
 $7(3) + 2(8) = 37$
 $21 + 16 = 37$
 $37 = 37$

4) $4x + 3y = 27$
 $y = 2x - 1$

D $4x + 3y = 27$
 C $4x + 3(2x - 1) = 27$
 M $4x + 6x - 3 = 27$
 S $10x - 3 = 27$
 $\quad +3 \quad +3$
 $\frac{10x = 30}{10 \quad 10}$
 $x = 3$

$y = 2x - 1$
 $y = 2(3) - 1$
 $y = 6 - 1$
 $y = 5$
 $(3, 5)$

chk#1 (3,5)
 $4x + 3y = 27$
 $4(3) + 3(5) = 27$
 $12 + 15 = 27$
 $27 = 27$

chk#2 (3,5)
 $y = 2x - 1$
 $5 = 2(3) - 1$
 $5 = 6 - 1$
 $5 = 5$

5) $x = -6y - 7$
 $3x + y = 13$

D $3x + y = 13$
 C $3(-6y - 7) + y = 13$
 M $-18y - 21 + y = 13$
 S $-17y - 21 = 13$
 $\quad +21 \quad +21$
 $\frac{-17y = 34}{-17 \quad -17}$
 $y = -2$

$x = -6y - 7$
 $x = -6(-2) - 7$
 $x = 12 - 7$
 $x = 5$
 $(5, -2)$

chk#1 (5,-2)
 $x = -6y - 7$
 $5 = -6(-2) - 7$
 $5 = 12 - 7$
 $5 = 5$

chk#2 (5,-2)
 $3x + y = 13$
 $3(5) + (-2) = 13$
 $15 - 2 = 13$
 $13 = 13$