

Solving Systems of Equations Day II: Using Substitution

I. Steps:

1. Replace what x or y are equal to into the other equation in place of the appropriate letter.
2. Solve the remaining equation.
3. Solve for the missing variable.
4. Do two checks.

II. Practice: Solve for the missing variables and check.

1. $3y - 2x = 11$
 $y = 9 - 2x$

$$\begin{aligned} 3y - 2x &= 11 \\ 3(9 - 2x) - 2x &= 11 \\ 27 - 6x - 2x &= 11 \\ 27 - 8x &= 11 \\ \underline{-27} & \quad \underline{-27} \\ -8x &= -16 \\ \underline{-8} & \quad \underline{-8} \\ x &= 2 \end{aligned}$$

$$\begin{aligned} y &= 9 - 2x \\ y &= 9 - 2(2) \\ y &= 9 - 4 \\ y &= 5 \end{aligned}$$

$(2, 5)$

Check #1
 $(2, 5)$
x y

$$\begin{aligned} 3y - 2x &= 11 \\ 3(5) - 2(2) &= 11 \\ 15 - 4 &= 11 \\ 11 &= 11 \end{aligned}$$

Check #2
 $(2, 5)$
x y

$$\begin{aligned} y &= 9 - 2x \\ 5 &= 9 - 2(2) \\ 5 &= 9 - 4 \\ 5 &= 5 \end{aligned}$$

2. $y = 5x - 7$
 $3x - 4y = -6$

$$\begin{aligned} 3x - 4y &= -6 \\ 3x - 4(5x - 7) &= -6 \\ 3x - 20x + 28 &= -6 \\ -17x + 28 &= -6 \\ \underline{-28} & \quad \underline{-28} \\ -17x &= -34 \\ \underline{-17} & \quad \underline{-17} \\ x &= 2 \end{aligned}$$

$$\begin{aligned} y &= 5x - 7 \\ y &= 5(2) - 7 \\ y &= 10 - 7 \\ y &= 3 \end{aligned}$$

$(2, 3)$

Check #1
 $(2, 3)$
x y

$$\begin{aligned} y &= 5x - 7 \\ 3 &= 5(2) - 7 \\ 3 &= 10 - 7 \\ 3 &= 3 \end{aligned}$$

Check #2
 $(2, 3)$
x y

$$\begin{aligned} 3x - 4y &= -6 \\ 3(2) - 4(3) &= -6 \\ 6 - 12 &= -6 \\ -6 &= -6 \end{aligned}$$

$$3. \quad 3y + 2x = 16$$

$$x = 2y + 1$$

$$3y + 2x = 16$$

$$3y + 2(2y + 1) = 16$$

$$3y + 4y + 2 = 16$$

$$\begin{array}{r} 7y + 2 = 16 \\ -2 \quad -2 \\ \hline \end{array}$$

$$\begin{array}{r} 7y = 14 \\ \frac{7y}{7} = \frac{14}{7} \end{array}$$

$$y = 2$$

$$x = 2y + 1$$

$$x = 2(2) + 1$$

$$x = 4 + 1$$

$$x = 5$$

$$(5, 2)$$

Check #1

$$(5, 2)$$

x, y

$$3y + 2x = 16$$

$$3(2) + 2(5) = 16$$

$$6 + 10 = 16$$

$$16 = 16$$

Check #2

$$(5, 2)$$

x, y

$$x = 2y + 1$$

$$5 = 2(2) + 1$$

$$5 = 4 + 1$$

$$5 = 5$$

$$4. \quad 2y - x = 10$$

$$x = -y + 2$$

$$2y - x = 10$$

$$2y - 1(-y + 2) = 10$$

$$2y + y - 2 = 10$$

$$\begin{array}{r} 3y - 2 = 10 \\ +2 \quad +2 \\ \hline \end{array}$$

$$\begin{array}{r} 3y = 12 \\ \frac{3y}{3} = \frac{12}{3} \end{array}$$

$$y = 4$$

$$x = -y + 2$$

$$x = -(4) + 2$$

$$x = -4 + 2$$

$$x = -2$$

$$(-2, 4)$$

Check #1

$$(-2, 4)$$

x, y

$$2y - x = 10$$

$$2(4) - (-2) = 10$$

$$8 + 2 = 10$$

$$10 = 10$$

Check #2

$$(-2, 4)$$

x, y

$$x = -y + 2$$

$$-2 = -(4) + 2$$

$$-2 = -4 + 2$$

$$-2 = -2$$